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$$\epsilon = \frac{1}{4\pi k}$$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0}$$

$$Q_{enc} = Q$$

$$\begin{aligned} \oint \vec{E} \cdot d\vec{A} &= \iint \vec{E} \cdot d\vec{A} \\ &= \iint E dA \\ &= E \iint dA \\ &= E(4\pi r^2) \end{aligned} \quad \left. \begin{array}{l} E(4\pi r^2) \\ = \frac{Q}{\epsilon_0} \end{array} \right\}$$

$$\vec{E} = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$$



$$\rho = \frac{Q}{\frac{4}{3}\pi a^3}$$

On GS

$$\vec{E} \parallel \vec{A}$$

E uniform

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0} = \frac{Q}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{A}$$

$$= \oint E dA$$

$$= E \oint dA = E(4\pi r^2)$$

$$\vec{E} = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$$



$$\rho = \frac{Q}{\frac{4}{3}\pi a^3} \quad \text{on GS}$$

$$\vec{E} \parallel \vec{A}$$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0} \quad | \quad E \text{ uniform}$$

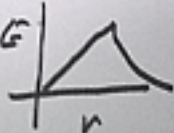
$$Q_{\text{enc}} = \iiint \rho \cdot dV$$

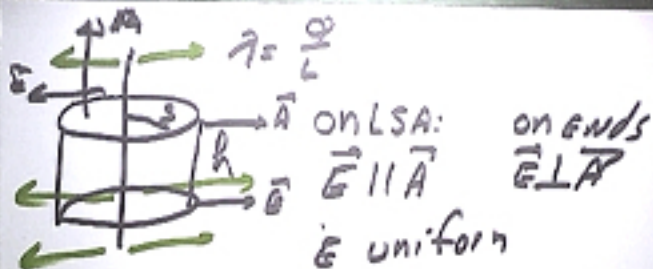
$$= \rho \iiint dV$$

$$= \rho \left[\frac{4}{3}\pi r^3 \right] \quad E$$

$$\oint \vec{E} \cdot d\vec{A} = E(4\pi r^2)$$

$$\vec{E} = \frac{\rho}{3\epsilon_0} \vec{r} = \frac{Q}{4\pi\epsilon_0 a^3} \frac{r}{a} \hat{r}$$





$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0} = \frac{\lambda h}{\epsilon_0}$$

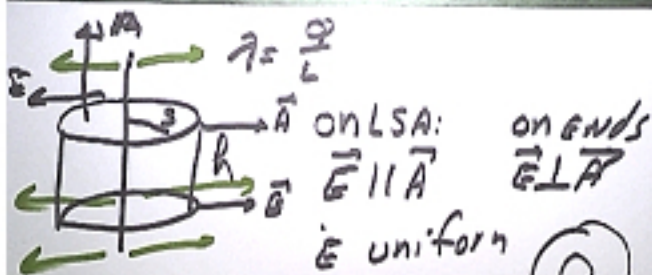
$$\oint \vec{E} \cdot d\vec{A} = \oint_{\text{ends}} \vec{E} \cdot d\vec{A} + \oint_{\text{LSA}} \vec{E} \cdot d\vec{A}$$

$$\oint_{\text{ends}} \vec{E} \cdot d\vec{A} = 0 \quad \oint_{\text{LSA}} \vec{E} \cdot d\vec{A}$$

$$= \oint E dA$$

$$= E \oint dA = E(2\pi sh)$$

$$E = \frac{\lambda h}{2\pi\epsilon_0 sh} \Rightarrow \boxed{\frac{\lambda}{2\pi\epsilon_0 s} \hat{s} = \vec{E}}$$

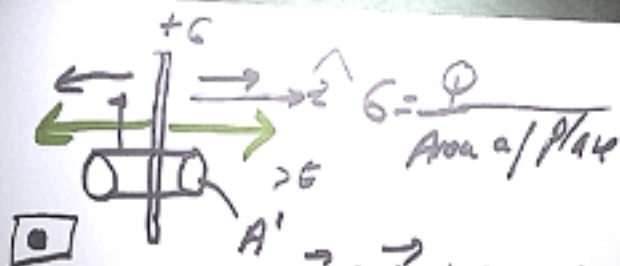


$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0} = \frac{\lambda h}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{A} = \oint_{ends} \vec{E} \cdot d\vec{A} + \oint_{LSA} \vec{E} \cdot d\vec{A}$$

$$= \oint_{LSA} E dA = E \oint dA = E(2\pi sh)$$

$$E = \frac{\lambda h}{2\pi\epsilon_0 sh} \Rightarrow \boxed{\frac{2}{2\pi\epsilon_0 s} \hat{s} = \vec{E}}$$



ON ENDS: $\vec{E} \parallel \vec{A}$; E uniform

ON LSA: $\vec{E} \perp \vec{A}$

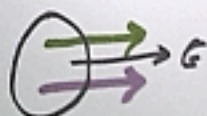
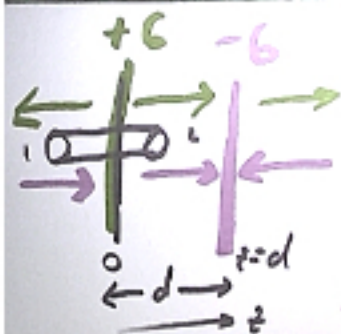
$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0} \quad Q_{\text{enc}} = G A'$$

$$\oint \vec{E} \cdot d\vec{A} = \oint_{\text{LSA}} \vec{E} \cdot d\vec{A} + \oint_{\text{ENDS}} \vec{E} \cdot d\vec{A}$$

$$= \oint \vec{E} \cdot d\vec{A} = \oint E dA = E \oint dA$$

$$= 2EA' \quad 2EA' = \frac{GA'}{\epsilon_0}$$

$$\vec{E} = \frac{G}{2\epsilon_0} \begin{cases} +\hat{z}; z > 0 \\ -\hat{z}; z < 0 \end{cases}$$



①

$$\vec{\Phi} = \vec{\Phi} + \vec{\Phi} + \vec{\Phi}$$

$\vec{\Phi}$ $\vec{\Phi}$ $\vec{\Phi}$
 ① LSA ②

0

②
on LSA: $\vec{E} \perp \vec{A}$

on ①: $\vec{E} = \vec{0}$

on ②: $\vec{E} \parallel \vec{A}$, E uniform

$$\begin{aligned}\vec{\Phi} &= \oint \vec{E} \cdot d\vec{A} = \oint E dA \\ &= E \oint dA = EA'\end{aligned}$$

$$Q_{enc} = 6A'$$

$$EA' = \frac{6A'}{\epsilon_0} \Rightarrow \vec{E} = \frac{6}{\epsilon_0} \hat{z}$$

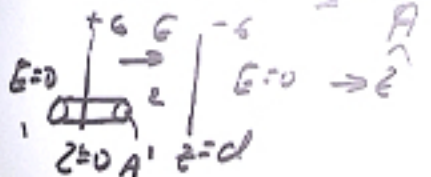
$$Q_{enc} = \sigma A'$$

$$\epsilon A' = \frac{\sigma A'}{\epsilon_0} \Rightarrow \vec{E} = \frac{\sigma}{\epsilon_0} \hat{z}$$

$$E=0 \quad \left| \begin{array}{c} \frac{\sigma}{\epsilon} \hat{z} \\ \rightarrow \end{array} \right| \quad E=0$$

again 11

$$\underline{E} = \frac{\Phi}{A}$$



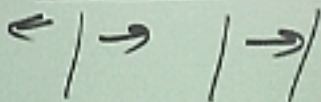
on GS: $\odot 2: \vec{E} \parallel \vec{A}; E$ uniform

$$\begin{aligned} \oint_{\vec{E}} \vec{E} \cdot d\vec{A} &= \oint E dA \\ &= E \oint dA = EA' \end{aligned}$$

$$Q_{enc} = \epsilon_0 EA' \Rightarrow EA' = \frac{QA'}{\epsilon_0}$$

$$\vec{E} = \frac{Q}{\epsilon_0 A'} \hat{z} \text{ (between)}$$

$$\vec{E} = \vec{0} \text{ outside}$$



$$\textcircled{1a} \quad \rho = C \cdot r$$

$$Q = \iiint \rho \, d^3r$$

if spherical symmetry

$$\iiint \rho \, d^3r = 4\pi \int_0^r \rho \cdot [r^2 dr]$$

$$= 4\pi C \int_0^r r \cdot r^2 dr$$

$$= 4\pi C \int_0^r r^3 dr \quad \left| \begin{array}{l} C = \frac{Q}{4\pi r^4} \end{array} \right.$$

$$\underline{\underline{\frac{4\pi C r^4}{4} = \pi C r^4}}$$

$$\textcircled{1a} \quad \rho = C \cdot r$$

$$Q = \iiint \rho \, d^3r$$

if Spherical Symmetry

$$\iiint \rho \, d^3r = 4\pi \int_0^r \rho \cdot [r^2 dr]$$

$$= 4\pi C \int_0^a r \cdot r^2 dr$$

$$= 4\pi C \int_0^a r^3 dr \quad \left| \begin{array}{l} C = \frac{Q}{4\pi a^4} \end{array} \right.$$

$$\frac{4\pi C a^4}{4} = \pi C a^4 \quad \left| \begin{array}{l} \text{stop} \end{array} \right. \div \epsilon_0 (4\pi r^2)$$