

**Instructions: You have a total of 55 minutes to complete this test.**

**Answer each question completely showing complete details.**

**For complete credit you must include correct SI units with numerical answers.**

Time Start \_\_\_\_\_ Time finish \_\_\_\_\_ pledged \_\_\_\_\_

Constants:  $k=8.987 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}$ ;  $\epsilon_0=8.854 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2}$ ;  $\mu_0=4\pi \times 10^{-7} \frac{\text{Tm}}{\text{A}}$

**(1)** Consider the circuit shown below. Provide correct Kirchoff's law equations for the following:

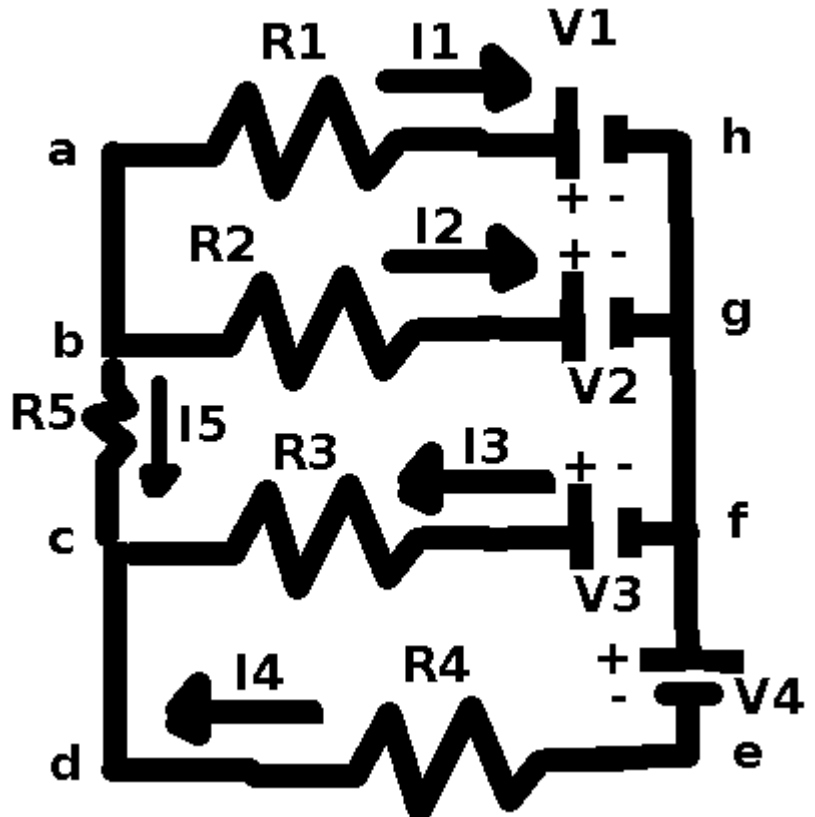
Loop (abgha): \_\_\_\_\_

Loop (bcfgb): \_\_\_\_\_

Loop (cdefc): \_\_\_\_\_

@b: \_\_\_\_\_

@c: \_\_\_\_\_



**Suppose the following values exist:**

resistances:  $R1=1\Omega$ ,  $R2=2\Omega$ ,  $R3=4\Omega$ ,  $R4=4\Omega$ ,  $R5=5\Omega$

Potentials:  $V1=10\text{V}$ ,  $V2=20\text{V}$ ,  $V3=30\text{V}$ ,  $V4=40\text{V}$

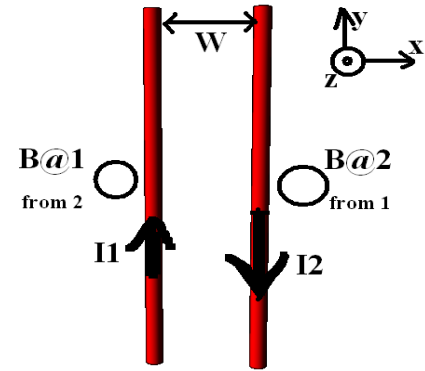
If the solutions for the currents are:

$I1=1.06\text{A}$ ,  $I2=-3.94\text{A}$ ,  $I3=1.81\text{A}$ ,  $I4=-10.78\text{A}$ ,  $I5=1.81\text{A}$

Calculate the total power radiated by the circuit

What is the interpretation of the result provided for current I4?

(2) Two long wires each of length  $L$  are separated by a distance  $w$  carry currents  $I_1$  and  $I_2$  in the directions shown. Note that  $x$  and  $y$  are in the plane of the wire while  $z$  comes out of the page.



(a) In the circles provided, show the direction of the magnetic fields,  $B@1$  from 2 and  $B@2$  from 1.

(b) Sketch, and label, force on wire 1 ( $F_1$ ) and the force on wire 2 ( $F_2$ ) on the diagram.

(c) Showing complete details, calculate the magnitude of the magnetic field at wire 2 (due to the current in wire 1). Your answer is in terms of  $I_1$ , and  $W$ .

(d) Calculate the magnitude of the force per unit length on wire 2 in terms of  $I_1$ ,  $I_2$ ,  $W$  and a constant.

(e) Suppose  $I_1=1$  A,  $I_2=2$  A, and  $W=1$ m. Provide a numerical result (with the correct unit vector direction, and correct SI units) for the force per unit length on wire 2.

**(3)** A parallel plate capacitor has one plate of area  $A$  located at  $z=0$  and the other plate of area  $A$  located at  $z=d$ . There is a surface charge  $+\sigma$  on the plate at  $z=0$  and  $-\sigma$  on the plate at  $z=d$ . Your answer should include sketches as needed.

**(a)** Calculate the electric field between the plates of the parallel plate capacitor in terms of  $\sigma$  and  $\epsilon_0$ .

**(b)** Calculate the magnitude of the potential difference between the plates.

**(c)** Calculate the total amount of charge separated,  $Q$  in terms of  $\sigma$  and  $A$ .

**(d)** Calculate the capacitance of the parallel plate capacitor in terms of  $\epsilon_0$ ,  $A$  and  $d$ .

**(e)** A capacitor is charged to a maximum charge  $Q$ . Find the total energy ( $U$ ) stored in the capacitor in terms of  $E$ ,  $\epsilon_0$ ,  $A$  and  $d$ .

**(f)** From your expression for the total stored energy ( $U$ ) obtained in (d), find an expression for the energy density inside the parallel plate capacitor in terms of  $\epsilon_0$  and  $E$ .

**(4) Note: in your answers below, be sure to include correct SI units.**

Resistor 1 has a resistivity  $\rho_1=5 \Omega\text{m}$  and a length  $L=0.1 \text{ m}$ . Resistor 2 has a resistivity  $\rho_2=10 \Omega\text{m}$  and a length  $L=0.2 \text{ m}$ . Both resistors have a cross sectional area  $A=0.1 \text{ m}^2$ .

**(a)** If the two resistors are placed in parallel, find the equivalent resistance.

**(b)** If the two resistors are placed in series, find the equivalent resistance.

Capacitor 1 has area  $A=0.1\text{m}^2$  and a plate separation  $d_1=0.1\text{m}$ . Capacitor 2 has an area  $A=0.1\text{m}^2$  and a plate separation  $d_2=0.2\text{m}$ .

**(c)** if the two capacitors are placed in parallel, find the equivalent capacitance.

**(d)** if the two capacitors are placed in series, find the equivalent capacitance.

**(e)** Suppose that a resistor  $R=1 \times 10^6 \Omega$  is placed in series with a capacitor  $C=33 \mu\text{f}$ . Calculate the time constant of this RC circuit.