

Instructions: You have a total of 55 minutes to complete this test.

Answer each question completely showing complete details.

For complete credit you must include correct SI units with numerical answers.

Time Start _____ Time finish _____ pledged _____

Constants: $k=8.987 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}$; $\epsilon_0=8.854 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2}$; $\mu_0=4\pi \times 10^{-7} \frac{\text{Tm}}{\text{A}}$

(1) Consider the circuit shown below. Provide correct Kirchoff's law equations for the following:

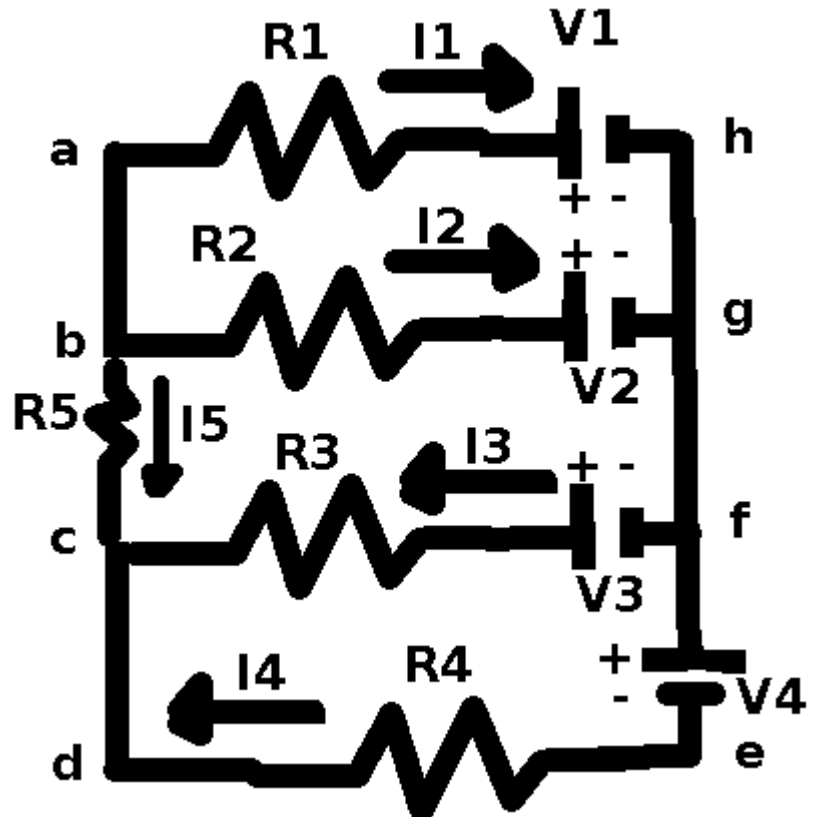
Loop (abgha): _____

Loop (bcfgb): _____

Loop (cdefc): _____

@b: _____

@c: _____



Suppose the following values exist:

resistances: $R_1=1\Omega$, $R_2=2\Omega$, $R_3=4\Omega$, $R_4=4\Omega$, $R_5=5\Omega$

Potentials: $V_1=10\text{V}$, $V_2=20\text{V}$, $V_3=30\text{V}$, $V_4=40\text{V}$

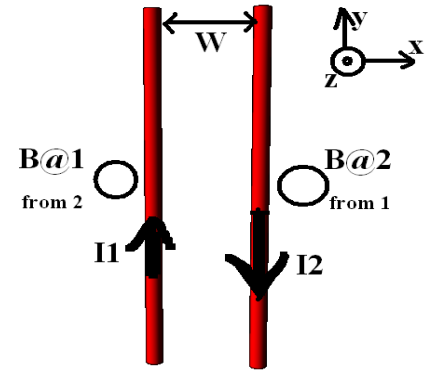
If the solutions for the currents are:

$I_1=1.06\text{A}$, $I_2=-3.94\text{A}$, $I_3=1.81\text{A}$, $I_4=-10.78\text{A}$, $I_5=1.81\text{A}$

Calculate the total power radiated by the circuit

What is the interpretation of the result provided for current I4?

(2) Two long wires each of length L are separated by a distance w carry currents I_1 and I_2 in the directions shown. Note that x and y are in the plane of the wire while z comes out of the page.



(a) In the circles provided, show the direction of the magnetic fields, $B@1$ from 2 and $B@2$ from 1.

(b) Sketch, and label, force on wire 1 (F_1) and the force on wire 2 (F_2) on the diagram.

(c) Showing complete details, calculate the magnitude of the magnetic field at wire 2 (due to the current in wire 1). Your answer is in terms of I_1 , and W .

(d) Calculate the magnitude of the force per unit length on wire 2 in terms of I_1 , I_2 , W and a constant.

(e) Suppose $I_1=1$ A, $I_2=2$ A, and $W=1$ m. Provide a numerical result (with the correct unit vector direction, and correct SI units) for the force per unit length on wire 2.

(3) A parallel plate capacitor has one plate of area A located at $z=0$ and the other plate of area A located at $z=d$. There is a surface charge $+\sigma$ on the plate at $z=0$ and $-\sigma$ on the plate at $z=d$. Your answer should include sketches as needed.

(a) Calculate the electric field between the plates of the parallel plate capacitor in terms of σ and ϵ_0 .

(b) Calculate the magnitude of the potential difference between the plates.

(c) Calculate the total amount of charge separated, Q in terms of σ and A .

(d) Calculate the capacitance of the parallel plate capacitor in terms of ϵ_0 , A and d .

(e) A capacitor is charged to a maximum charge Q . Find the total energy (U) stored in the capacitor in terms of E , ϵ_0 , A and d .

(f) From your expression for the total stored energy (U) obtained in (d), find an expression for the energy density inside the parallel plate capacitor in terms of ϵ_0 and E .

(4) Note: in your answers below, be sure to include correct SI units.

Resistor 1 has a resistivity $\rho_1=5 \Omega\text{m}$ and a length $L=0.1 \text{ m}$. Resistor 2 has a resistivity $\rho_2=10 \Omega\text{m}$ and a length $L=0.2 \text{ m}$. Both resistors have a cross sectional area $A=0.1 \text{ m}^2$.

(a) If the two resistors are placed in parallel, find the equivalent resistance.

(b) If the two resistors are placed in series, find the equivalent resistance.

Capacitor 1 has area $A=0.1\text{m}^2$ and a plate separation $d_1=0.1\text{m}$. Capacitor 2 has an area $A=0.1\text{m}^2$ and a plate separation $d_2=0.2\text{m}$.

(c) if the two capacitors are placed in parallel, find the equivalent capacitance.

(d) if the two capacitors are placed in series, find the equivalent capacitance.

(e) Suppose that a resistor $R=1 \times 10^6 \Omega$ is placed in series with a capacitor $C=33 \mu\text{f}$. Calculate the time constant of this RC circuit.