

Sample calculations for lab 07

Here, I want you to study how the results that give the period are obtained.
Follow through these calculations (writing them on a sheet of paper.)

A mass m is attached to the end of a string of length L forming a simple pendulum. Initially the mass is at an angle θ_0 .

Period of the simple pendulum

The torque on the pendulum is initially given by (assuming the end of the string to be the pivot point:

I: Torque about the axis: $\vec{\Gamma} = \vec{R} \times \vec{F} \Rightarrow |(\vec{\gamma})| = -|\vec{R}||\vec{F}|\sin(\theta)$

II: small angle approximation: if θ is small, then $\sin(\theta) \approx \theta$

III: response of system to the torque: it produces a time rate of change in angular momentum or: $\Gamma = I\alpha$ where I is the moment of inertia. The moment of inertia about the pivot is $I = mL^2$.

From this find α in terms of the torque. $mL^2\alpha = -Lmg\sin(\theta) \Rightarrow \alpha \approx \frac{-g}{L}\theta$

IV: Equation of motion: Write the resulting equation in "standard form" as $\alpha + \frac{g}{L}\theta = 0$.

Recall that the general solution to this type of equation is: $\theta = \theta_0 \cos(\omega t)$; $\omega = \sqrt{\frac{g}{L}}$ when the pendulum is at an amplitude.

V: From ω , find the period, T , of the simple pendulum when $L = 1$ m.

$T =$ _____

Period of the Spring mass system

A mass m is connected to a spring of spring constant k . The system is held horizontal in the Earth's gravitational field.

I: the spring exerts a force on the mass given by: $F = -kx$ (ignoring the - sign here).

II: the mass responds to this force by Newton's laws: $F = ma$

III: Equate these to obtain the equation of motion in standard form:

$$ma = -kx \Rightarrow a + \frac{k}{m}x = 0$$

IV: Recognize the solution to this is: $x = A \cos(\omega t)$; $\omega = \sqrt{\frac{k}{m}}$ when the mass is initially at an amplitude.

V: From this find the period, T , of the spring mass system when $k = 1$ N/m and $m = .5$ kg.

$T =$ _____